The Crystal Structure of Te₃Nb₂O₁₁

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Te₃Nb₂O₁₁ crystallizes in space group $P2_12_12$ with a = 7.700(2), b = 15.700(3), c = 3.980(1) Å, and Z = 2. Full matrix least squares refinement gave an R value of 0.033 using 521 independent reflections. Infinite double Nb–O octahedra, sharing corners, are connected *via* finite



strings, to form a three-dimensional net. The threefold coordinated Te(IV) atom has the normal pyramidal configuration (Te-O = 1.84, 1.86 and 1.86 Å), while the fourfold coordinated Te(IV) atom has an unusual configuration in which the centre of the Te(IV) atom is placed within a tetrahedron of oxygen atoms. The average Nb-O bond distance of 2.00 Å is normal. However, the Nb atom is displaced from the centre of the oxygen octahedron along the polar axis (chain direction), to give alternating short and long Nb-O distances of 1.80 Å and 2.19 Å, respectively.

Introduction

A variety of structural building units have been found in different tellurate(IV) compounds and discussed by Zemann (1) and by the present authors (2, 3). Usually Te(IV) has a one-sided three- or fourfold coordination of oxygen atoms. The most simple unit is the pyramidal TeO₃²⁻ ion which is present in $K_2TeO_3 \cdot 3H_2O$ (4). Other isolated units containing two or more tellurium(IV) atoms have also been found, e.g. groups of composition Te₂O₅, Te₃O₈ and Te₄O₁₁, containing central chains



* Permanent address: Department of Inorganic Chemistry, Chalmers' University of Technology and the University of Göteborg, Fack, S-402 20 Göteborg 5, Sweden. etc. The Te₂O₅ unit was first found in 1965 by Walitzi (5) in the mineral denningite, and later also in CuTe₂O₅ (6), Te₂V₂O₉ (7) and Cr₂Te₄O₁₁ (8). The only known structure containing the Te₃O₈ unit is Zn₂Te₃O₈, which was investigated by Hanke (9) in 1966. Infinite sheets are present in Te₂O₃SO₄ (10). In α -TeO₂ (11) and β -TeO₂ (12) the tellurium and oxygen atoms are connected to form three-dimensional network structures.

It is well known that the geometry of the TeO_3 unit (and the TeO_4 unit, when fourcoordinated) is strongly dependent on the character of the metal atom in different Metellurates. This is probably due to the polarizability of the Te(IV) free electron pair. It is now of interest to investigate whether the central $\cdots Te-O-Te\cdots$ configuration in more condensed tellurates(IV) is stable, or if it is as easily affected by the structural environment as is the TeO_3 coordination polyhedron.

We chose to work with the Nb₂O₅-TeO₂ system, since it would appear to be possible to prepare single crystals of a niobium tellurate(IV) with a structure similar to that of Te₂V₂O₉. The preparation of three different phases in the Nb₂O₅-TeO₂ system, namely TeNb₆O₁₇, Te₂Nb₂O₉ and Te₄Nb₂O₁₃ has been described by Guillaume (13).

Experimental

Starting from the composition $1Nb_2O_5: 2TeO_2$, single crystals of a niobium tellurate(VI) were obtained in a sealed gold tube at a temperature of 750°C. The crystal quality, cell dimensions and space group extinctions were first investigated on a precession camera. The collection of integrated intensities was performed with an automatic 4-circle diffractometer, CAD-4. Important crystal data and constants, and the settings of the diffractometer are given in Table I.

TABLE I

EXPERIMENTAL DATA

1.	Physical and crystallographic data	
	Formula: Te ₃ Nb ₂ O ₁₁	Molecular weight: 744.6
	Crystal system: orthorhombic	Space group: $P2_12_12$
	a = 7.700(2) Å	$V = 481 \text{ Å}^3$
	b = 15.700(3)	Z = 2
	c = 3.979(1)	F(000) = 326
	Absorption factor: $(MoK\alpha) = 116 \text{ cm}^{-1}$	$\rho_X = 5.14 \text{ g} \cdot \text{cm}^{-3}$
	Morphology: parallelepiped;	
	$0.0030 \times 0.0048 \times 0.0012$ cm	
2.	Data collection	
	Temperature: 20°C	
	Radiation: $MoK\alpha = 0.71069$ Å	
	Monochromator: oriented graphite crystal	
	Crystal-detector distance: 208 mm	
	Detector window ^a : height = 3 mm, width = $2.10 + 1.0$	$\tan\theta$ mm
	Take off angle ^{<i>a</i>} : 3.0°	
	Scan mode: omega	
	Maximum bragg angle (θ): 30°	
	Scan angle: $\theta = \theta_0 + B \cdot \tan \theta$	B = 0.35
	Values determining scan speed: ^{a} SIGPRE = 0,400	SIGMA = 0.018
	$VPRE = 10^{\circ}/min$	TMAX = 80 sec
	Controls: Intensity	Orientation
	Reflections: $1 4 0, 0 \overline{3} 1, 0 10 0 3 \overline{7}$	1, 0 10 0, 3 4 1
	Periodicity: 3600 sec 5	0 reflections
3.	Conditions for refinement	
	Reflections for the refinement of cell dimensions: 25	
	Recorded reflections: 924	
	Independent reflections: 787	
	Significant reflections: 521	
	Refined parameters: 75	
	Reliability factors: $R = \sum k F_0 - F_c / \sum k$	$ F_0 = 0.033$
	$R_{w} = \left[\sum w^{2}(k F_{0} - F_{c})\right]$	$(5) w^{2} k^{2} F_{0}^{1} = 0.036$

^a Cf. A. Mossett, J. J. Bonnet, and J. Galy, Acta Cryst., B 33, 2639-2644 (1977).

Structure Determination and Absolute Configuration

It was possible to index the powder diagram reported for $Te_2Nb_2O_9$ by Guillaume (13) with the parameters refined on the CAD-4 diffractometer, using 25 strong *hkl* reflections (cf. Table II). The structure determination was then commenced assuming that there were two formula units of $Te_2Nb_2O_9$ in the cell. In the Patterson

TABLE II POWDER PATTERN OF Te₃Nb₂O₁₁

hkl	$d_{\rm obs}({\rm \AA})$	$d_{\rm calc}({\rm \AA})$	<i>I/I</i> 0
110	6.90	6.91	7
130	4.33	4.33	25
001	3.98	3.98	65
{011	3.853	3.858	30
200	0.000	3.850	50
210	3.735	3.739	90
{021	3 534	3.550	50
{101	5.554	3.536	50
140	3.497	3.497	100
{111	3.453	3.457	90
1220	000	3.449	20
121	3.222	3.224	65
031	3.166	3.168	70
230	3.097	3.101	7
131	2.928	2.930	60
150	2.908	2.908	60
041	2.794	2.795	10
211	2.722	2.725	20
221	2.609	2.610	45
160	2.479	2.478	20
320	2.439	2.440	10
151	2.348	2.348	7
330	2.302	2.304	7
251	2.076	2.076	20
002	1.990	1.990	20
071	1.955	1.954	15
410	1.910	1.911	15
261	1.889	1.901	30
122	1.870	1.871	7
(420		1.870	
032	1.860	1.860	7
212	1.754	1.757	7
280	1.749	1.748	7
440	1.727	1.728	7
411	1.722	1.722	10

function most of the predominant peaks could be explained assuming that the Te and Nb atoms were situated in two general positions $P2_12_12:4(c)$. However, it was also evident that there were two further Te atoms in the twofold position 2(a). Thus the formula is $Te_3Nb_2O_{11}$ rather than $Te_2Nb_2O_9$. Assuming that the Te(IV) free electron pair occupies the same volume as an oxygen atom (14, 15), the new formula corresponds to an average volume of 17.2 Å³/oxygen atom, which agrees well with previously observed values. It proved possible to identify oxygen peaks in the successive electron density maps in accordance with the formula $Te_3Nb_2O_{11}$.

A preliminary refinement of the atomic positions and isotropic temperature factors gave an R value of 0.076. At this stage, an absorption correction was applied to the observations, using the program AGNOST. In the final refinement, which included anisotropic temperature factors and an isotropic extinction parameter, the R value dropped to 0.033 ($R_w = 0.036$). The refinement was performed with the full matrix least squares program NUCLS, adapted to the IRIS80 computer by Bonnet. Both the ordinary and the anomalous scattering factors were obtained from the "International Tables," Vol. IV (16). The observed structure factors were weighted using unmodified $\sigma(F)$ quantities calculated as $abs \cdot (2F \cdot Lp)^{-1} \cdot \sigma(I)$. Those reflections with $I \ge 2\sigma(I)$ were regarded as being significant. The final atomic parameters are given in Table III and a list of observed and calculated structure factors has been deposited.¹ The orientation given in Table III may be regarded as correct, since a refinement based on a set of identical parameters with reversed signs for the zcoordinates gave an R value of 0.036 ($R_w =$

¹ Structure factor tables have been deposited with the National Auxilary Publications Service (NAPS), P.O. Box 3513, Grand Central Station, New York 10017.

Final Atomic Parameters for $Te_3Nb_2O_{11}^{a}$									
Atom	x	у	z	$\boldsymbol{\beta}_{11}$	β ₂₂	β ₃₃	β ₁₂	β_{13}	β ₂₃
Te (1)	0.3104(2)	0.2978(1)	0.8619(4)	52(2)	12(1)	114(8)	3(1)	0(5)	-1(2)
Te(2)	1/2	1/2	0.1443(6)	164(5)	18(1)	70(12)	-27(2)	0	0
Nb	0.3717(2)	0.1014(1)	0.2493(5)	44(3)	7(1)	50(9)	1(1)	10(6)	1(3)
0(1)	0.355(2)	0.107(1)	0.699(4)	92(30)	34(7)	143(110)	25(14)	-11(52)	7(25)
0(2)	0.247(2)	0.217(1)	0.181(4)	32(22)	18(7)	292(129)	18(10)	-30(49)	18(24)
0(3)	1/2	0	0.200(5)	95(41)	17(8)	41(155)	-13(17)	0	0
0(4)	0.140(2)	0.044(1)	0.187(4)	109(33)	26(7)	342(143)	-32(13)	10(65)	-7(26)
0(5)	0.579(2)	0.172(1)	0.198(5)	70(28)	40(9)	454(159)	-45(14)	-57(58)	5(33)
0(6)	0.360(2)	0.385(1)	0.157(4)	104(32)	24(7)	313(116)	-8(13)	-1(68)	-30(26)

TABLE III FINAL ATOMIC PARAMETERS FOR $Te_3Nb_2O_{11}^a$

^a The ansotropic temperature factor is given as $\exp[-(h^2\beta_{11}+k^2\beta_{22}+l^2\beta_{33}+2hk\beta_{12}+2hl\beta_{13}+2kl\beta_{23})\cdot 10^4]$.

0.039). The $R_w(xy\bar{z})/R_w(xyz)$ ratio is thus 1.083, which is significant according to Hamilton's (17) *R*-value test ($\mathcal{R}_{1,454,0.005} =$ 1.005). 1.73–2.31 Å found in Nb₂O₅ by Gatehouse and Wadsley (18). The average Nb-O distance of 2.00 Å also compares well with the corresponding value of 1.99 Å in Nb₂O₅.

Discussion of the Structure

A projection of the structure on the (001)plane is shown in Fig. 1. Interatomic bond distances and angles are listed in Table IV. The niobium atom is octahedrally coordinated by oxygen atoms, while the tellurium(IV) coordination is of two kinds: one Te(IV) atom is threefold pyramidally coordinated while the other has a fourfold coordination. The structure is best described in terms of infinite, double chains of niobium-oxygen octahedra sharing corners (cf. Fig. 2). These chains are cross-linked by finite

chains. The tellurium atoms are also bonded to oxygen atoms in the Nb–O octahedra, thus forming a three-dimensional net structure with Nb–O octahedral chains and Te_3O_8 groups, as indicated in Fig. 1.

The niobium-oxygen coordination distances (Table IV) all lie within the range



FIG. 1. Projection of the structure of $Te_3Nb_2O_{11}$ onto the (001) plane. The different polyhedra NbO_6 (octahedron), $Te(1)O_3E(1)$ (tetrahedron) and $Te(2)O_4E(2)$ (trigonal bipyramid) share corners only (E = Te(IV) free electron pair).

INTERATOMIC BOND DISTANCE	S AND ANGLES IN TO3N02011
Te(1)-O(2) : 1.86(2) Å	O(2)-O(4) : 2.83(2) Å
Te(1)-O(51): 1.86(2)	O(2)–O(5) : 2.65(2)
Te(1)-O(6) : 1.84(2)	O(2)–O(51) : 2.64(2)
Te(2)-O(41): 1.84(2)	O(2)–O(6) : 2.78(2)
Te(2)-O(42): 1.84(2)	O(3)–O(4) : 2.86(2)
Te(2)-O(6) : 2.10(2)	O(3)–O(5) : 2.76(2)
Te(2)-O(60) : 2.10(2)	O(41)-O(42) : 2.47(3)
Nb-O(1) : 1.80(1)	O(41)–O(6) : 2.78(2)
Nb-O(1) : 2.19(1)	O(42)–O(6) : 2.85(2)
Nb-O(2) : 2.07(1)	O(51)–O(6) : 2.73(2)
Nb-O(3) : 1.885(3)	
Nb-O(4) : 2.01(1)	
Nb-O(5) ¹ : 1.95(1)	
O(1)–O(2) : 2.82(2)	$O(2)-Te(1)-O(51): 90.6(7)^{\circ}$
O(1)–O(3) : 2.83(2)	O(2)-Te(1)-O(6) : 97.2(7)
O(1)-O(4) :2.80(2)	O(51)-Te(1)-O(6) : 95.1(8)
O(1)-O(5) : 2.83(2)	
O(1')-O(2) : 2.71(2)	O(41)-Te(2)-O(42): 88.4(9)
O(1')-O(3) :2.83(2)	O(6) -Te(2)-O(60) : 182.8(9)
O(1')–O(4) : 2.73(2)	
O(1')-O(5) : 2.82(2)	Te(1)-O(6)-Te(2) : 136.6(9)

TABLE IV

EANORS AND ANOTES IN TAINLOUS

^a The notation is in accordance with Fig. 1.

The Nb-Nb distance across the chains in $Te_3Nb_2O_{11}$ is 3.784 Å, which is in good agreement with the value 3.822 Å in Nb_2O_5 . However, along the chains in $Te_3Nb_2O_{11}$, the



FIG. 2. Infinite double chains of NbO_6 octahedra sharing corners.

Nb-Nb distance is longer and is identical with the *c*-axis separation, i.e. 3.979 Å. It is interesting to note that the shortest and longest Nb-O distances of 1.80 Å and 2.19 Å, respectively, also occur alternatingly in the \cdots O-Nb-O-Nb \cdots chain along the c axis (cf. Fig. 2). The corresponding displacement of the niobium atom from the central plane in the oxygen octahedron is 0.22 Å. A similar árrangement exists in ferroelectric barium sodium niobate whose structure has been determined by Jamieson, Abrahams, and Bernstein (19). In this structure there are four independent niobium atoms in the asymmetric unit of space group Cmm2. The displacements of the niobium atoms from the central oxygen planes lie in the range 0.17-0.21 Å, all in the same direction in the crystal. The corresponding Nb-Nb distance is also increased, being 3.99 Å. However, Te₃Nb₂O₁₁ cannot exhibit spontaneous ferroelectricity, since it belongs to space group $P2_12_12$, which is without a polar direction.

The threefold coordinated Te(1) atom has pyramidal relatively symmetrical а arrangement of oxygen atoms (Table IV). This indicates that the nonbonded electron pair of Te(1) is essentially unaffected by the surrounding oxygen atoms. Accordingly the shortest Te-O distance, behind Te(1), is 3.03 Å. The coordination of Te(1) agrees well with that of the TeO_3^{2-} ion in $K_2TeO_3 \cdot 3H_2O$ (4), in which the average value for the Te-O bond length is 1.85 Å. It also fits well in the general scheme described for the (18+2) shell ions Ge(II)...Bi(III) (15, 20).

The fourfold coordinated Te(2) atom in Te₃Nb₂O₁₁ lies on a twofold rotation axis, which is also the case in α -TeO₂ (11) and in Zn₂Te₃O₈ (9). This type of coordination is usually described as a trigonal bipyramid with one of the equatorial positions occupied by the Te(IV) free electron pair.

It is useful to describe the free electron pair as a sphere with a volume similar to that of an oxygen atom (15). Although the volume does not appear to alter appreciably (15) it is reasonable to assume that the packing of oxygen atoms around the free electron pair leads to distortion from spherical symmetry, i.e. the free electron pair becomes polarized. Zemann (1) has demonstrated that there are preferred orientations of the fifth and sometimes even the sixth nearest oxygen atoms on the "backside" of the fourcoordinated tellurium(IV) atom.

The structural arrangement of the oxygen atoms in contact with the free electron pair, i.e. on the "backside" of the tellurium atom, influences the repulsion between the free electron pair and the Te- O_{eq} and Te- O_{ax} bonding electron pairs. Usually this leads to O_{ax} -Te- O_{ax} and O_{eq} -Te- O_{eq} angles of about 165° and 100° instead of the regular trigonal bipyramidal angles of 180° and 120° (Fig. 3). The different values of these angles exhibited in the structures listed in Table V indicate that the free electron pair is strongly polarizable.



FIG. 3. Schematic representations of the tellurate(IV) trigonal bipyramide: (a) As usually found (cf. Table V); (b) As found in $Te_3Nb_2O_{11}$.

A new feature of the trigonal bipyramidal configuration in Te₃Nb₂O₁₁ is that it is not one-sided but Te-O_{ax} is slightly bent towards the Te(IV) free electron pair (cf. Fig. 3 and Table V). The oxygen atoms around Te(2) and its free electron pair in Te₃Nb₂O₁₁ form a distorted hexagonal bipyramid, and from Fig. 4 it would appear that the free electron pair is elongated in the plane of the equatorial bonds. This ought to lead to increased repulsion in the equatorial plane, but have a lesser effect on the axial bonds, which fits well with the structural results obtained.

On both sides of Te(2), the axial atom O(6) is also bonded to Te(1), resulting in a Te₃O₈ group. This building unit has been previously studied only in $Zn_2Te_3O_8$ (9). The arrangement of the central

chain is similar in the two structures, both having a twofold symmetry axis through the central Te atom. The Te-O-Te angle in some different tellurates(IV) containing Te_2O_5 and Te_3O_8 groups are compared in Table VI. The variations indicate that the Te-O-Te bridge, in a similar manner to the oxygen coordination of a single Te(IV) atom, is relatively easily affected by the surrounding structural arrangement.

Acknowledgments

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Compound	Te-O _{eq}	Te–O _{ax}	O_{eq} -Te- O_{eq}	O_{ax} -Te- O_{ax}	Ref.
α-TeO ₂	2×1.90(2) Å	2×2.10(2) Å	102°	169°	(11)
Te ₂ O ₅	1.892(6), 1.913(4)	2.072(5), 2.080(6)	91	166	(21)
$Zn_2Te_3O_8$	$2 \times 1.83(3)$	$2 \times 2.10(3)$	106	175	(9)
$Te_3Nb_2O_{11}$	$2 \times 1.84(2)$	$2 \times 2.10(2)$	86	183	
$H_2Te_2O_6$	1.861(6), 1.937(4)	2.065(5), 2.107(5)	91	172	(22)
$Te(C_6H_4O_2)_2$	1.98(2), 1.98(2)	2.01(3), 2.11(3)	98	154	(23)
$Te_2O_3(HPO_4)$	1.79(4), 1.99(4)	2.02(4), 2.12(4)	95	168	(24)
TiTe ₃ O ₈	$2 \times 1.85(2)$	$2 \times 2.12(2)$	102	159	(25)
Te ₂ O ₄ NHO ₃	1.88(2), 1.95(1)	2.02(2), 2.16(2)	100	148	(26)
$UO_2Te_3O_7$	1.78(4), 2.02(4)	2.15(4), 2.16(4)	96	157	(27)
β -TeO ₂	1.88(2), 1.93(2)	2.07(2), 2.19(2)	101	168	(12)

TABLE V Fourfold Oxygen Coordination of Tellurates $(IV)^a$

^a The compounds are listed in order of the longest Te-O_{ax} bond up to 2.20 Å.





FIG. 4. (a) The distorted hexagonal bipyramid around Te(2); (b) The packing of oxygen atom in the Te(2) equatorial plane.

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TABLE VI

Compound	Te-O-Te	O–Te distances	Ref.	
Cu Te ₂ O ₅	120.6(2)°	1.931(3), 2.019(3) Å	(6)	
$Zn_2Te_3O_8$	126.0 (2x)	1.98, 2.10	(9)	
$Te_2V_2O_9$	143.3(2)	1.921(3), 1.921(3)	(7)	
$(NH_4)_2Te_2O_52H_2O$	118.0(2)	2.030(3), 1.901(3)	(28)	
$Nb_2Te_3O_{11}$	132.1(9) (2x)	1.84(2), 2.10(2)		

Te-O-Te Angles in some Tellurates (IV)

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